

Proving and Explaining the Unfeasibility of Message Sequence Charts for Hybrid Systems

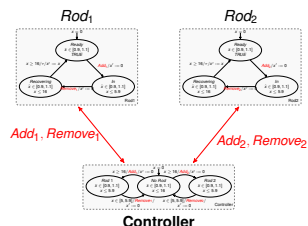
Alessandro Cimatti **Sergio Mover** Stefano Tonetta

Fondazione Bruno Kessler

October 31, 2011

Hybrid Systems

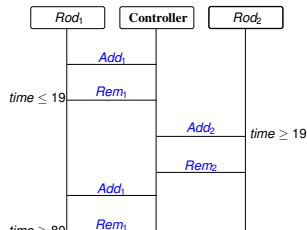
- Mix **discrete** (e.g. hardware) and **continuous** (e.g. sensor) behaviors.
- **Complex critical systems**: train control system (ETCS), airplane traffic control system (TCAS), ...
- **Network** of components.



Scenario-verification

Is there a run of the system compatible with the scenario?

If such a run exists, the scenario is **feasible**.



Existing approaches:

- 1 Reduction to **reachability**:
 - Can prove both feasibility and unfeasibility.
 - Inefficient.
- 2 **Scenario-based** encoding [CAV11]:
 - Cannot prove unfeasibility.
 - Efficient.

Our contribution is a **SMT**-based technique that:

- Efficiently proves **unfeasibility**.
- Extracts **explanations** for the unfeasibility.

- 1 Background
 - SMT analysis of Hybrid Systems
 - Scenario-Verification
- 2 Proving the unfeasibility of scenarios
- 3 Explanations of Unfeasibility
- 4 Experimental Evaluation
- 5 Conclusions and future work

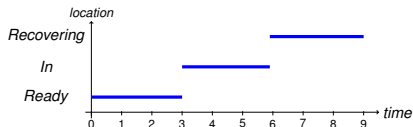
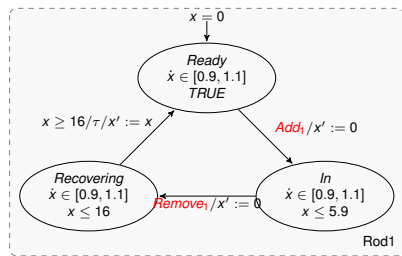
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Hybrid Automata

Hybrid automata ([Henzinger 96]):

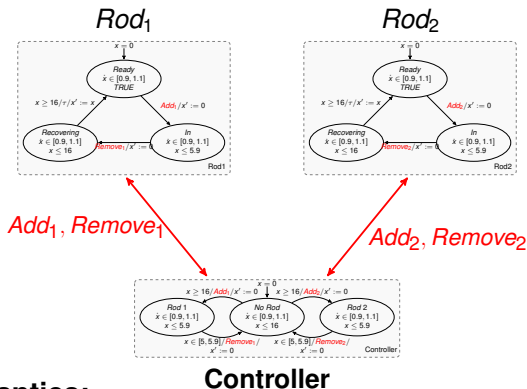
- Framework for representing hybrid systems.
- **Discrete** instantaneous mode switches.
- **Continuous** evolution according to flow conditions.



Hybrid Automata Network

Network of hybrid automata $\mathcal{H} = H_1 \parallel \dots \parallel H_n$:

- Move **asynchronously** on local events (τ).
- **Synchronize** on shared events.



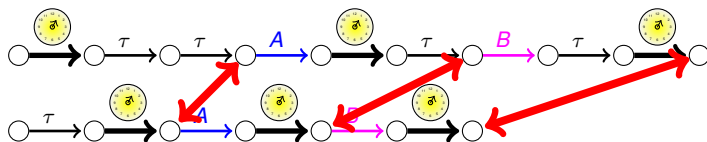
Different semantics:

- 1 Global-time ([Henzinger 96]).
- 2 **Local-time** ([Bengtsson 98]).

Controller

Local-time semantics

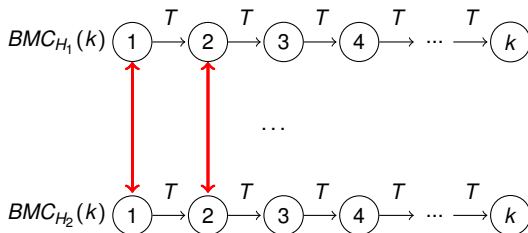
- The time evolves **independently** in each automaton:
 - Local time scale.
 - The continuous evolution is a **local transition**.
- The local time of the automata must be the same:
 - On synchronizations.
 - At the end of a run.



τ = local event (no stutter or time).

SMT analysis of Hybrid Systems

- Each automaton is encoded in a symbolic transition system $H_i = \langle \text{Init}_i, \text{Trans}_i \rangle$.
- Bounded model checking:



- **k-induction**.
 - Base case: BMC up to k .
 - Inductive case: BMC and **simple path condition** up to $k + 1$.
- Use **SMT** solvers as decision procedure.

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Constrained Message Sequence Charts

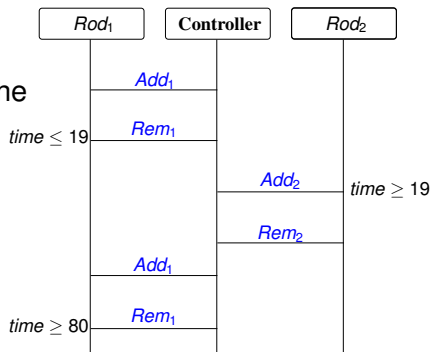
$\langle m, \phi \rangle$: Message sequence chart m with constraints ϕ .

m : parallel composition of instances.

$\phi = \phi_g \wedge \phi_1 \wedge \dots \wedge \phi_n$: formulas over the

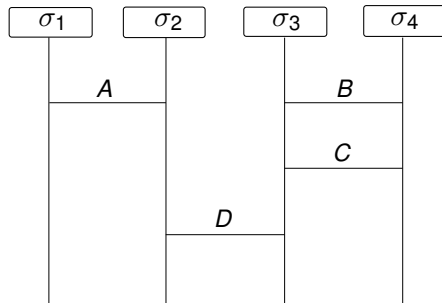
network variables **on synchronization**.

- Global (ϕ_g): over **all** the network variables.
- Local ϕ_i : over variable of H_i .

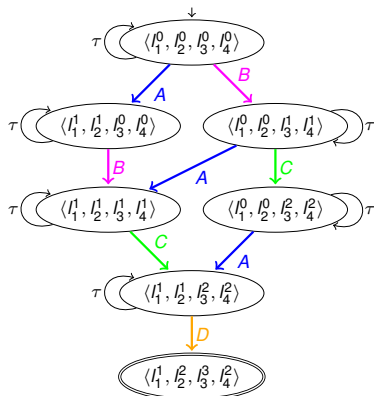


MSC verification via reachability

- The CMSC is translated in a monitor automaton S_m .
- The automaton is composed with the network.
- Enables off-the-shelf verification techniques:
 - BMC: feasibility.
 - k-induction: unfeasibility.

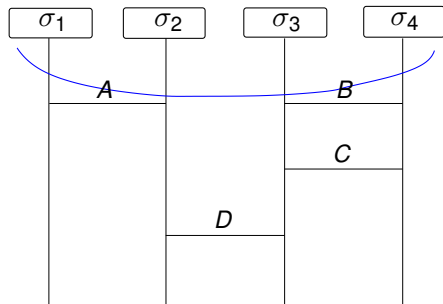


$$m = \sigma_1 || \sigma_2 || \sigma_3 || \sigma_4$$

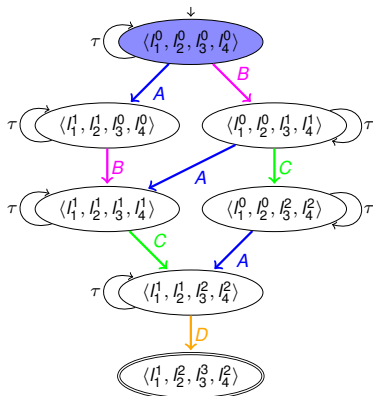


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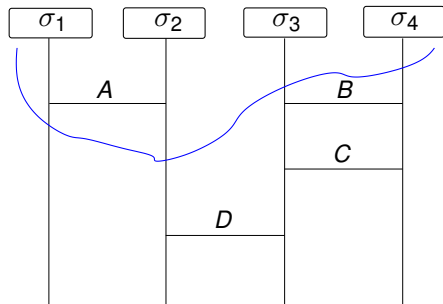


Cut: $\langle I_1^0, I_2^0, I_3^0, I_4^0 \rangle$

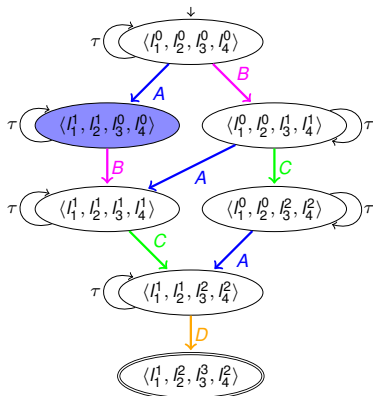


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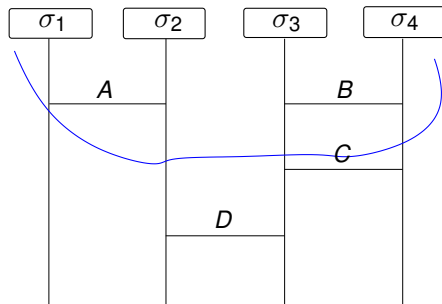


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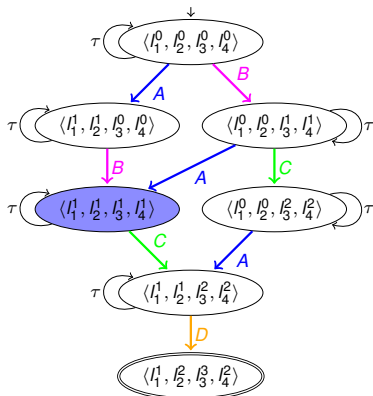


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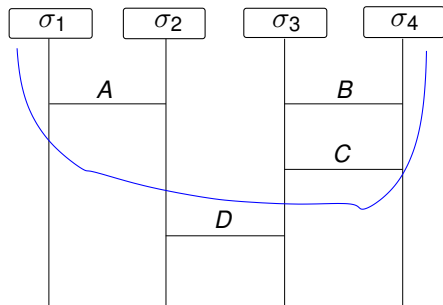


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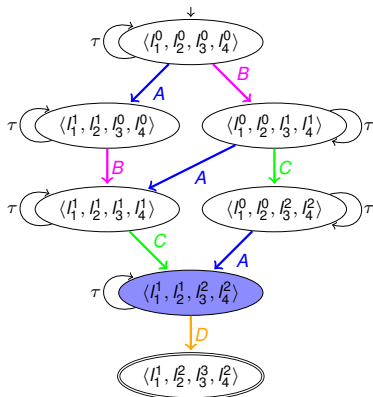


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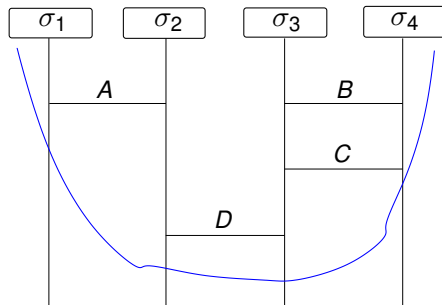


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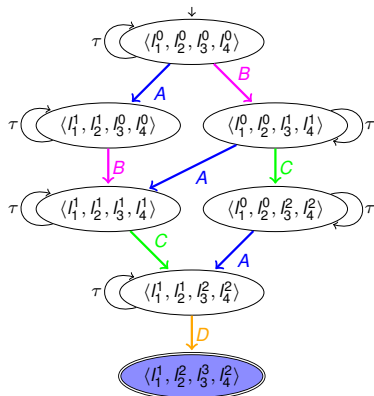


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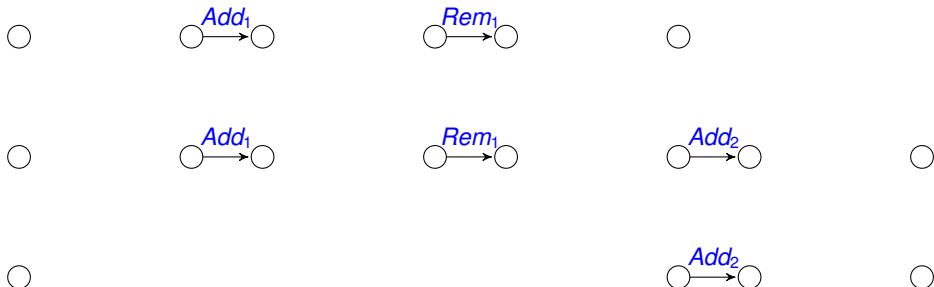
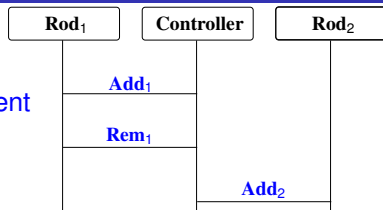


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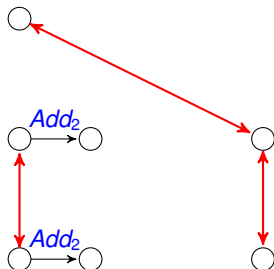
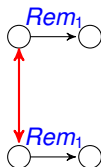
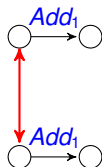
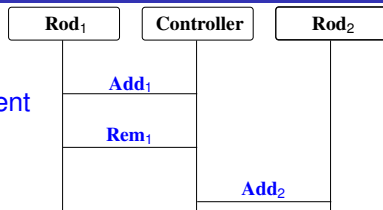
Scenario-based encoding

- For all the automata:
 - Fix the position of the shared events.
transitions are simplified wrt shared event



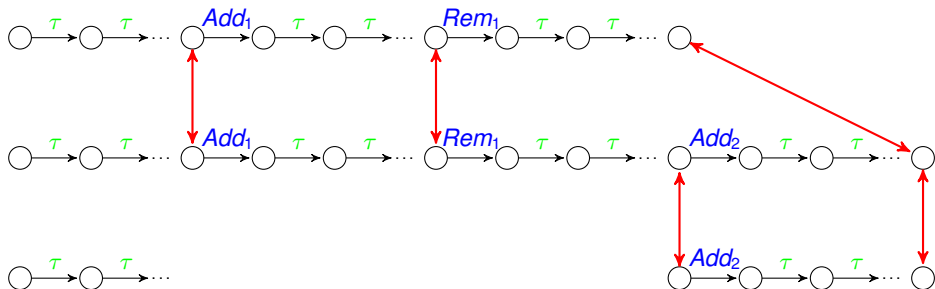
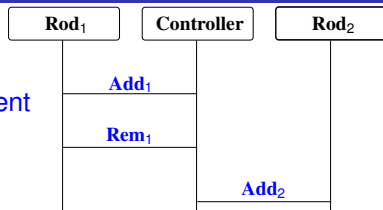
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 - Add the synchronization constraints.



Scenario-based encoding

- For all the automata:
 - Fix the position of the shared events.
transitions are simplified wrt shared event
 - Add the synchronization constraints.
 - Encode the “local segments”.
transitions are simplified wrt τ



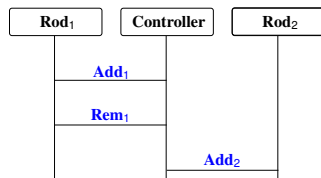
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Efficient unfeasibility check

	Reduction to reachability	SMT-based approach
Feasibility	BMC Inefficient	Scenario-driven encoding Efficient
Unfeasibility	K-induction Inefficient	Partitioned k-induction Efficient

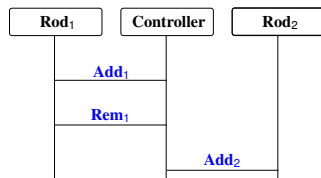
Partitioned K-induction - Algorithm

- **Inductive step**: proved incrementally following the partial order of the MSC.
- **Base case**: bounded feasibility check.



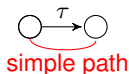
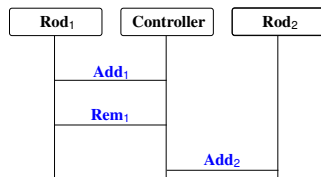
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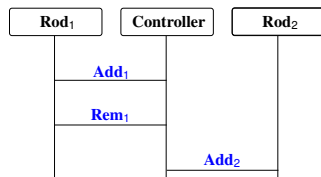
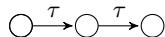


SAT - new states are reachable



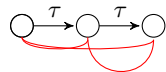
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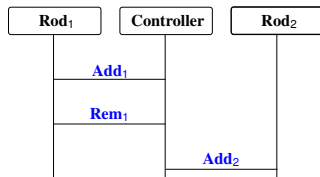
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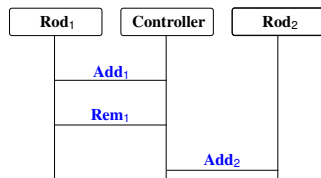
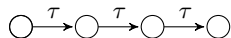
simple path

SAT - new states are reachable



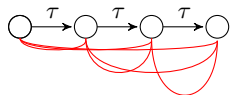
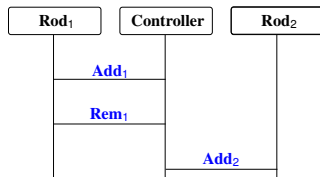
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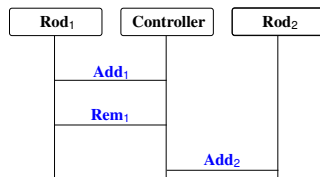
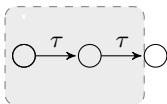
UNSAT - no new states are reachable

simple path



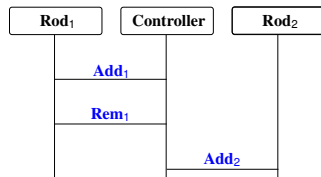
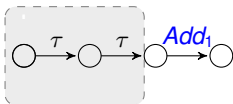
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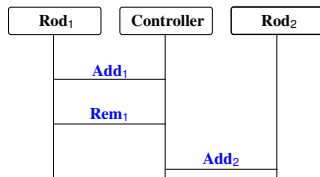
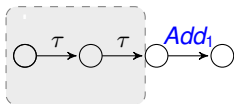
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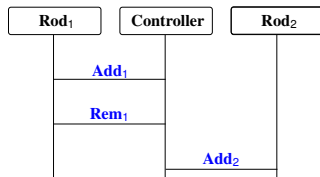
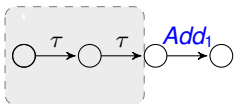
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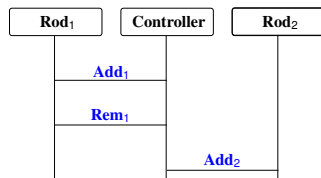
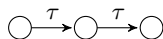
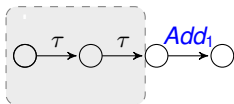
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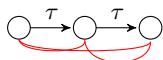
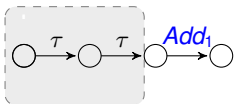
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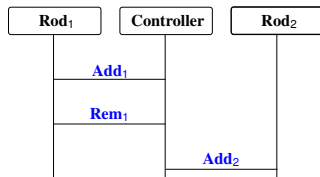
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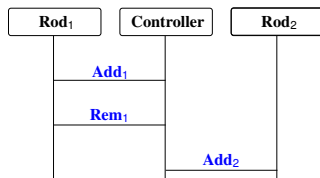
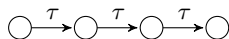
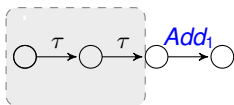
SAT - new states are reachable

simple path



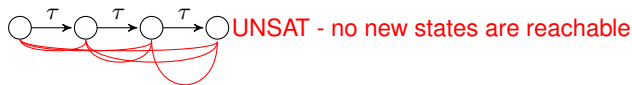
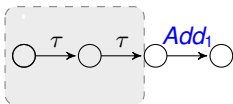
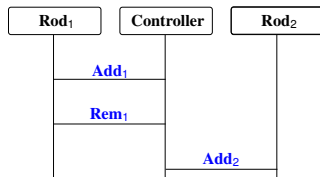
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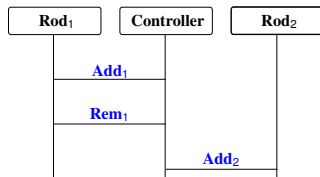
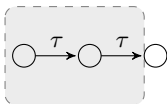
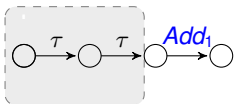
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○ simple path

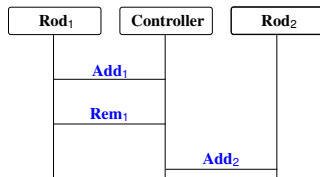
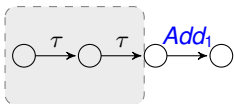
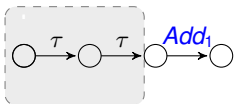
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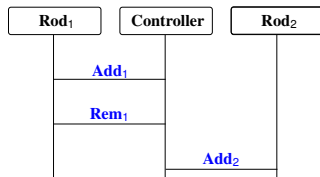
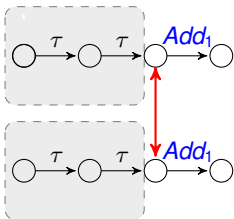
Partitioned K-induction - Algorithm

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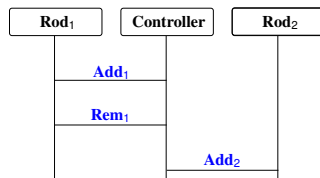
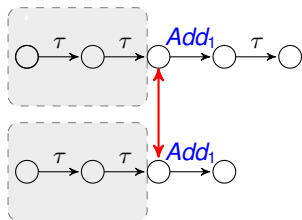
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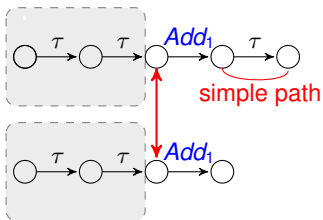
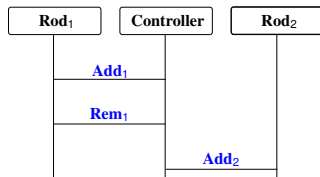
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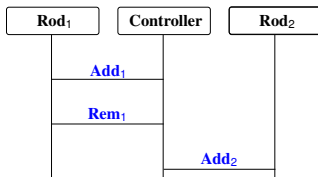
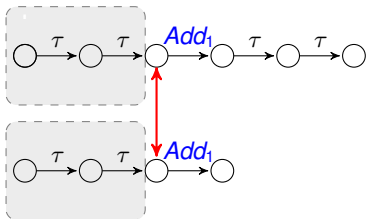


SAT - new states are reachable



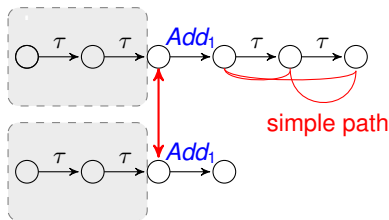
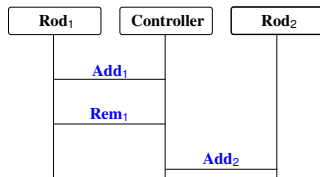
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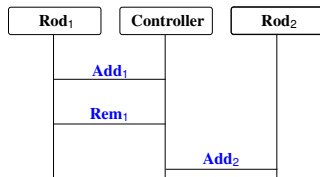
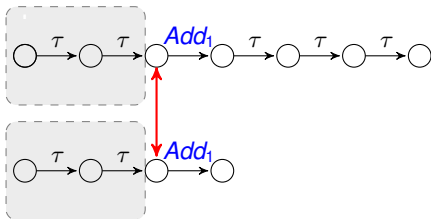


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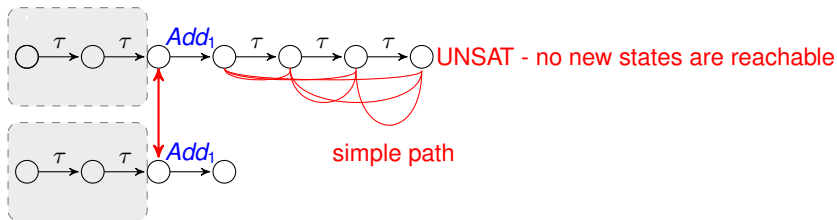
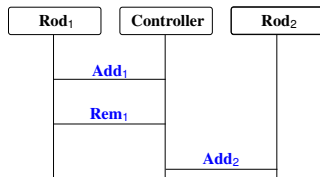
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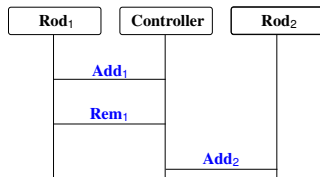
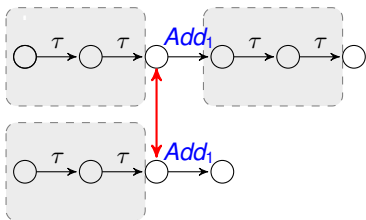
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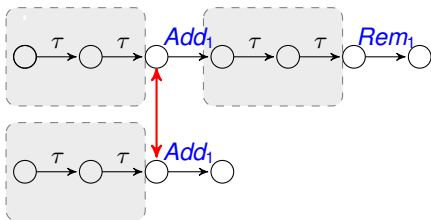
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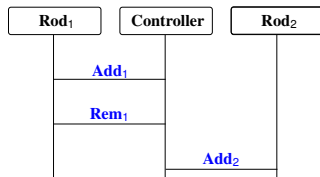


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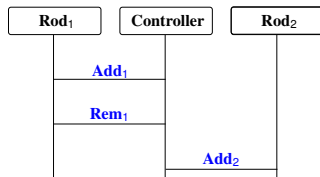
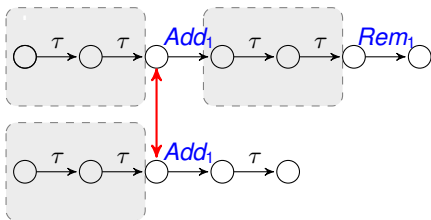


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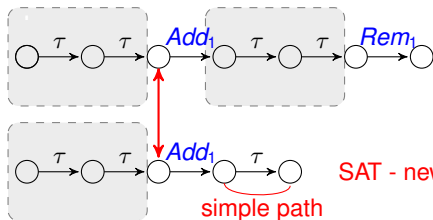
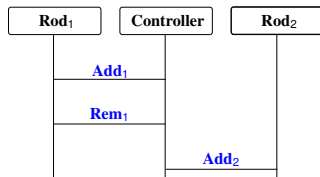
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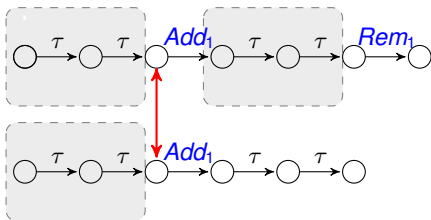
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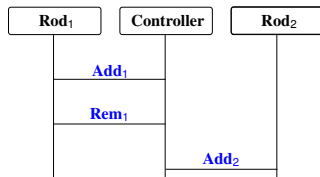


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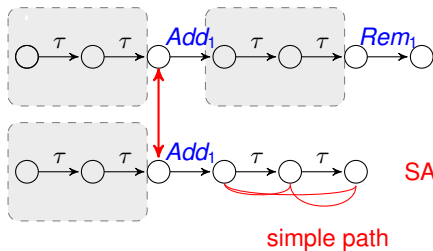
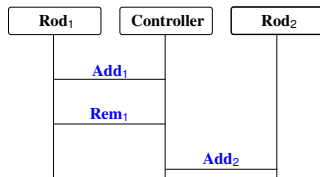


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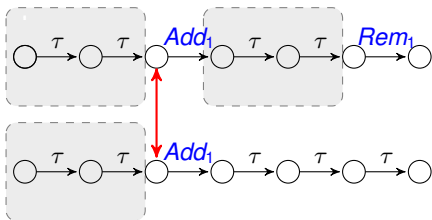
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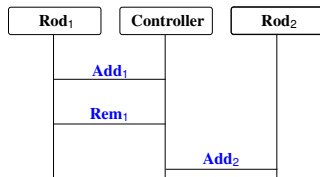


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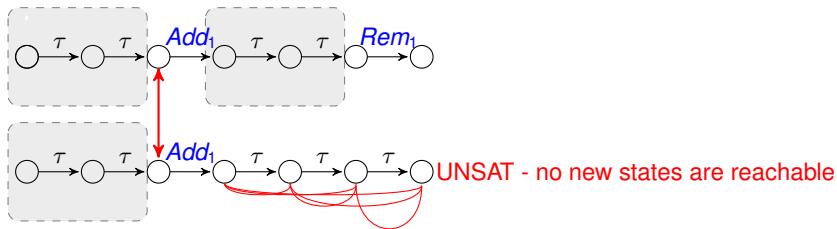
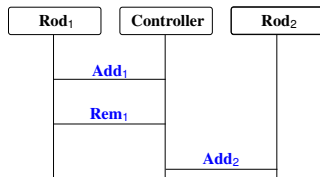


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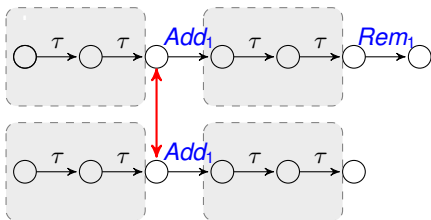


simple path

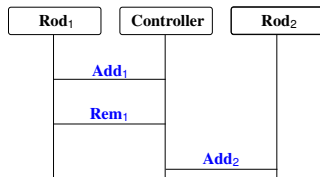


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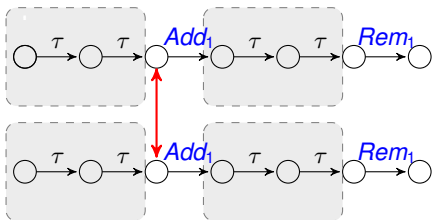


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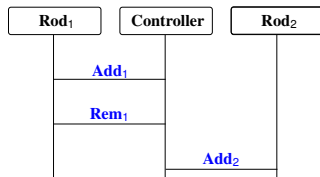


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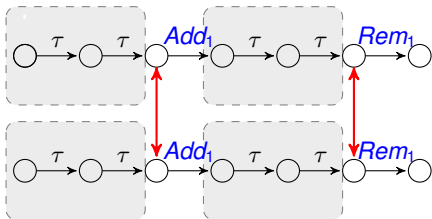


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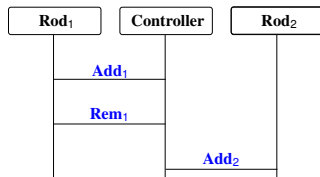


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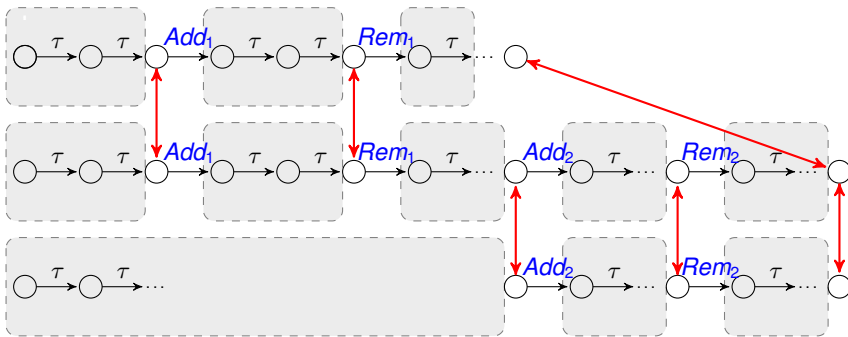
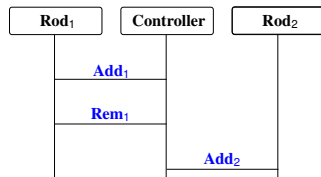


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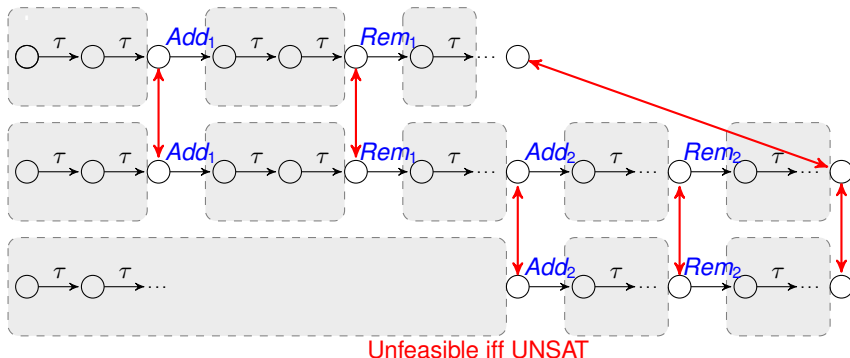
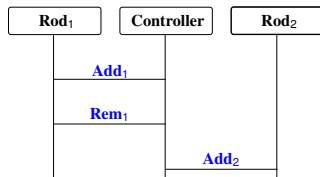
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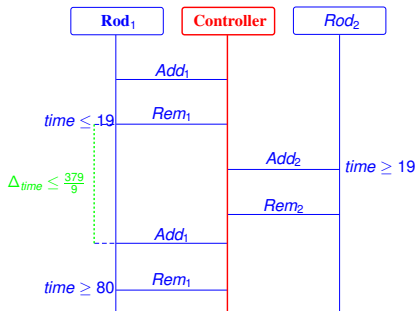
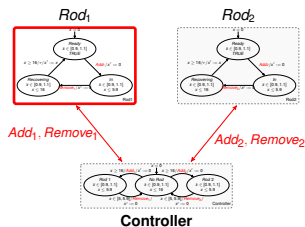
- 1 Background
 - SMT analysis of Hybrid Systems
 - Scenario-Verification
- 2 Proving the unfeasibility of scenarios
- 3 Explanations of Unfeasibility**
- 4 Experimental Evaluation
- 5 Conclusions and future work

- Typical use case:
 - We expect that a scenario is feasible.
 - The analysis proves that the scenario is unfeasible in the network.
 - How do we explain the unfeasibility?
- We extract three types of explanations for the unfeasibility.

Unfeasibility due to a component

Explained with a formula that:

- Is **required** by the component when simulating its MSC events.
- Is **not consistent** with the other components when they simulate the events of the MSC.



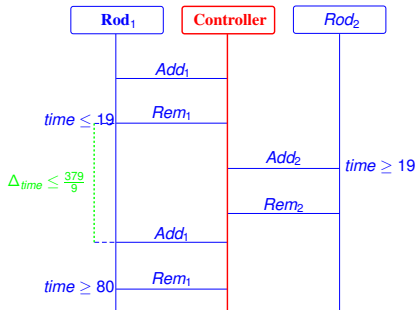
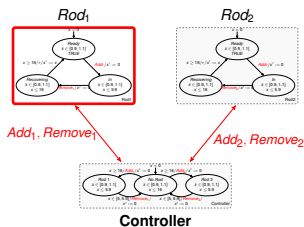
Unfeasibility due to a component

Explained with a formula that:

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It is the **interpolant** of **A** and **B**:

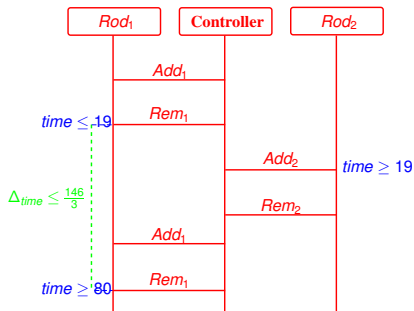
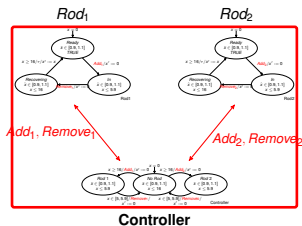
- **A** is the encoding of the component and its MSC events.
- **B** is the encoding of the other components and their MSC events.



Unfeasibility due the network

Explained with a formula that:

- Is **required** by the network when simulating the MSC.
- Is **not consistent** with the additional constraints of the MSC.



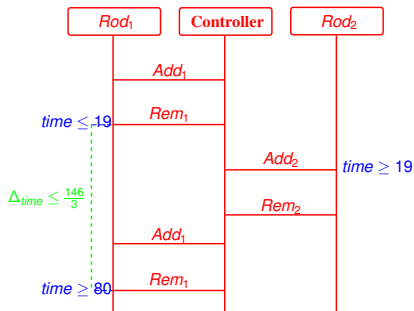
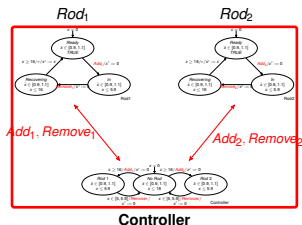
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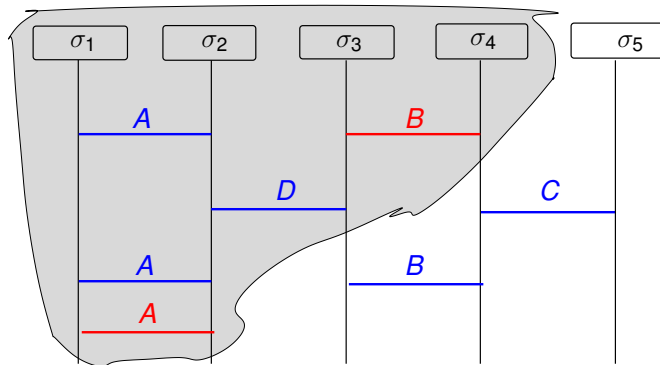
It is the **interpolant** of **A** and **B**:

- **A** is the encoding of the network and the MSC.
- **B** are the CMSC constraints.



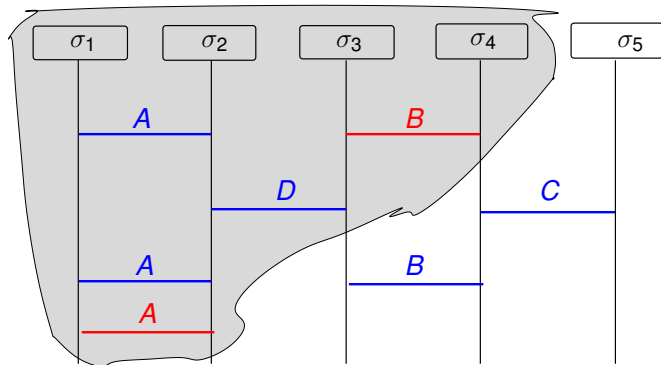
Inconsistent subset of the CMSC

Subset of the original CMSC that is still unfeasible with the network.



Inconsistent subset of the CMSC

Subset of the original CMSC that is still unfeasible with the network.
Extracted from the **unsatisfiable core** of the encoding.



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Implementation:

- Approach implemented on top of the NuSMV model checker.
- We use the MATHSAT SMT solver.

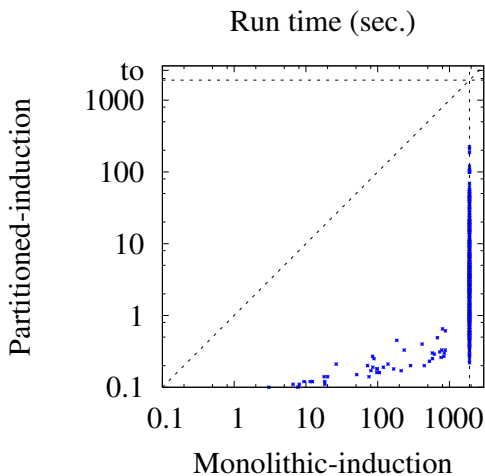
Settings:

- Linear hybrid automata benchmarks.
- Several handcrafted (unsatisfiable) MSCs.
- We scaled the dimension of the benchmarks (number of automata, length of the MSCs).

Comparison:

- MSC partitioned k-induction.
- Monolithic k-induction on the system composed with the monitor automata.

Partitioned k-induction vs. Monolithic k-induction (run times)



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Conclusions and future work

- Efficient approach for proving the unfeasibility of CMSC.
 - The encoding exploits the structure of the CMSC.
 - Partitioned k-induction.
- Unfeasibility explanations:
 - Useful to localize and correct the errors.
 - Extracted exploiting the SMT solver functionalities.

Future works:

- More expressive MSCs (e.g. partial MSCs specifications).
- Validate the extracted explanations by real users.
- Automatic refinement loop in the abstraction.
- Non-linear hybrid systems.

Thank you for your attention.